



# **Solving linear equations**

# Introduction

**Equations** occur in all branches of engineering. They always involve one or more unknown quantities which we try to find when we **solve** the equation. The simplest equations to deal with are **linear equations**. On this leaflet we describe how these are solved.

# 1. A linear equation

Linear equations are those which can be written in the form

$$ax + b = 0$$

where x is the unknown value, and a and b are known numbers. The following are all examples of linear equations.

3x + 2 = 0, -5x + 11 = 0, 3x - 11 = 0

The unknown does not have to have the symbol x, other letters can be used.

3t - 2 = 0, 7z + 11 = 0, 3w = 0

are all linear equations.

Sometimes you will come across a linear equation which at first sight might not appear to have the form ax + b = 0. The following are all linear equations. If you have some experience of solving linear equations, or of transposing formulas, you will be able to check that they can all be written in the standard form.

$$\frac{x-7}{2} + 11 = 0, \qquad \frac{2}{x} = 8, \qquad 6x - 2 = 9$$

# 2. Solving a linear equation

To solve a linear equation it will be helpful if you know already how to transpose or rearrange formulas. (See leaflets 2.10 & 2.11 Rearranging formulas, for information about this if necessary).

When solving a linear equation we try to make the unknown quantity the subject of the equation. To do this we may

- add or subtract the same quantity to or from both sides
- multiply or divide both sides by the same quantity



### Example

Solve the equation x + 7 = 18.

## Solution

We try to obtain x on its own on the left hand side.

$$x + 7 = 18$$
  
 $x = 18 - 7$  by subtracting 7 from both sides  
 $x = 11$ 

We have solved the equation and found the solution: x = 11. The solution is that value of x which can be substituted into the original equation to make both sides the same. You can, and should, check this. Substituting x = 11 in the left-hand side of the equation x + 7 = 18 we find 11 + 7 which equals 18, the same as the right-hand side.

#### Example

Solve the equation 5x + 11 = 22.

## Solution

5x + 11 = 22 5x = 22 - 11 by subtracting 11 from both sides $x = \frac{11}{5} by dividing both sides by 5$ 

#### Example

Solve the equation 13x - 2 = 11x + 17.

## Solution

13x - 2 = 11x + 17  $13x - 11x - 2 = 17 ext{ by subtracting } 11x ext{ from both sides}$  2x - 2 = 17  $2x = 17 + 2 ext{ by adding } 2 ext{ to both sides}$  2x = 19  $x = \frac{19}{2}$ 

#### Exercises

1. Solve the following linear equations.

a) 4x + 8 = 0, b) 3x - 11 = 2, c) 8(x + 3) = 64, d) 7(x - 5) = -56, e) 3c - 5 = 14c - 27.

#### Answers

1. a) x = -2, b)  $x = \frac{13}{3}$ , c) x = 5, d) x = -3, e) c = 2.

